

उत्तराखण्ड विद्यालयी शिक्षा परिषद, र

केन्द्र संख्या की मुहर **केन्द्र स्थापक के हस्ताक्षर**
हाईस्कूल
के 0 सं- 1691 *Misc an*

नोट-केन्द्र के नाम की मुहर उत्तरपुरितक के किसी भी भाग पर न लगाएं।

परीक्षार्थी द्वारा करा जायेगा-

अनुक्रमांक (अंको में) **22046342**

अनुक्रमांक (शब्दों में) *Two crore twenty two, forty six thousand three hundred forty two*
 विषय- **Maths**

प्रश्नपत्र संकेतांक- **231(106)**

परीक्षा का दिन- **Tuesday**

परीक्षा तिथि **05 April, 2022**

कक्ष निरीक्षक द्वारा करा जाय-

केन्द्र संख्या- **1691**

परीक्षा कक्ष संख्या **01**

उपरोक्त सभी प्रविष्टियों की जांच मेरे द्वारा सम्पत्तीयपूर्वक कर ली गयी है।

कक्ष निरीक्षक का नाम- **Neena-Nautiyal**

दिनांक **05/04/2022**

हरताक्षर कक्ष निरीक्षक- *Neena*

प्रमाणित किया जाता है कि मैंने इस उत्तरपुरितका का मूल्यांकन समुचित प्रश्न-पत्र संकेतांक तथा मूल्यांकन निर्देशों के अनुसार किया है। प्राप्तांकों का मुखपृष्ठ पर अग्रसारण कर प्राप्तांकों एवं प्राप्तांकों के योग का मिलान कर लिया गया है। एवार्ड ब्लैक में प्राप्तांकों की अंकना कर उनका पुनः मिलान भी कर लिया है। किसी भी प्रकार की त्रुटि के लिए मैं उत्तरदायी रहूँगा/रहूँगी।

परीक्षक के हस्ताक्षर एवं संख्या

1. अंकेशक के हरताक्षर एवं संख्या

2. अंकेशक के हरताक्षर एवं संख्या

सन्निरीक्षा प्रयोगार्थ

सन्निरीक्षा पूर्व अंक-

सन्निरीक्षा पश्चात् अंक-

त्रुटि का प्रकार-

दिनांक-

हरताक्षर निरीक्षक-

Qus. 1 Ans...

⇒ 21

Qus. 2 Ans...

⇒ 1

Qus. 3 Ans...

⇒ '616 cm²' will be the surface area of sphere whose diameter is 14 cm

Qus. 4 Ans...

⇒ $\angle B = 90^\circ$

Qus. 5 Ans...

⇒ A die is thrown once, probability of getting an odd no. on the top will be ' $\frac{1}{2}$ ' $\left[\frac{1}{2}\right]$ Answer

Qus. 6 Ans...

⇒ rational number ' $\frac{129}{2^2 \times 5^7 \times 7^5}$ ' will have non-terminating repeated decimal expansion.

Qus. 7 Ans.

⇒ Given, sum of zeroes = 0 i.e. $\alpha + \beta$
product of zeroes = $\sqrt{5}$ i.e. $\alpha\beta$

We know, polynomial;

$$x^2 - (\alpha + \beta)x + \alpha\beta$$

⇒ $x^2 - (0)x + \sqrt{5}$

⇒ $[x^2 + \sqrt{5}]$ is required polynomial

Qus. 8 Ans.

⇒ Given, quadratic equation;

$$x^2 - 4x + 4 = [ax^2 + bx + c] \text{ standard form}$$

To find, nature of roots;

$$\text{Discriminant} = b^2 - 4ac$$

$$\Rightarrow (-4)^2 - 4(1)(4)$$

$$\Rightarrow 16 - 16 = 0$$

∴, in given equation $b^2 - 4ac = 0$,
therefore, the quadratic equation
($x^2 - 4x + 4 = 0$) will have two
equal roots.

Qus. 9 Ans...

⇒ A circle can have infinitely many tangents.

Qus. 10 Ans...

⇒ Probability of a sure event is '1'

Qus. 11 Ans...

⇒ Let the larger number be 'x' and smaller no. be 'y'
∴ [such that $x > y$]

Then, according to question,

$$x - y = 26 \quad \rightarrow \textcircled{1}$$

Also, given, larger no. is three times the smaller

$$\Rightarrow x = 3y \quad \rightarrow \textcircled{2}$$

Putting this value in eqⁿ ①, we get

$$\Rightarrow 3y - y = 26$$

$$2y = 26$$

$$\Rightarrow [y = 13] \text{ Sol}^n$$

On putting 'y = 13' in eqⁿ ②, we obtain

$$[x = 3 \times 13 = 39] \text{ Sol}^n$$

Therefore, the two numbers are
39 & 13.

Qus 12. Ans...

$$\Rightarrow \text{Given, } \cos \theta = \frac{4}{5}$$

We know, $\cos \theta = \frac{\text{Base}}{\text{Hypotenuse}}$

$$\Rightarrow \frac{\text{Base}}{\text{Hypotenuse}} = \frac{4k}{5k} \quad \therefore \text{Base} = 4k$$
$$\text{Hypotenuse} = 5k$$

Such that, 'k' is any +ve integer

Then, according to pythagoras theorem:

$$(\text{Hypotenuse})^2 = (\text{Base})^2 + (\text{Perpendicular})^2$$

$$\Rightarrow (5k)^2 = (4k)^2 + (P)^2$$

$$\Rightarrow P = \sqrt{25k^2 - 16k^2}$$

$$P = \sqrt{9k^2} = 3k$$

or we can say:

$$\text{Perpendicular} = 3$$

Now, given, $(\cot \theta + \operatorname{cosec} \theta)^2$

$$\therefore \cot \theta = \frac{\text{Base}}{\text{Perpendicular}} = \frac{4k}{3k}$$

$$\operatorname{cosec} \theta = \frac{\text{Hypotenuse}}{\text{Perpendicular}} = \frac{5k}{3k}$$

$$\Rightarrow \left(\frac{4k}{3k} + \frac{5k}{3k} \right)^2 = \left(\frac{9k}{3k} \right)^2 = (3)^2 = \boxed{9} \text{ Answer}$$

Qus. 13 Ans...

\Rightarrow Given, coordinates: let ABC

$$A = (3, 2)$$

$$B = (-2, -3)$$

$$C = (2, 3) \text{ Using distance formula:}$$

$$\text{i.e. } \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

A.

We get,

$$AB = \sqrt{(-2-3)^2 + (-3-2)^2}$$

$$\Rightarrow \sqrt{(5)^2 + (5)^2} = \sqrt{25+25} = \sqrt{50} \text{ unit}$$

$$BC = \sqrt{(2+2)^2 + (3+3)^2}$$

$$\Rightarrow \sqrt{(4)^2 + (6)^2} = \sqrt{16+36} = \sqrt{52} \text{ unit}$$

$$AC = \sqrt{(2-3)^2 + (3-2)^2}$$

$$\Rightarrow \sqrt{(-1)^2 + (1)^2} = \sqrt{1+1} = \sqrt{2} \text{ unit}$$

Here, $AB + BC > AC$

i.e. $\sqrt{50} + \sqrt{52} > \sqrt{2}$

Also, Vice-versa,

Since, sum of any two sides is greater than third side, then coordinates can form a triangle. (Yes)

Triangle is a triangle because

Qus 14. Ans

⇒ In provided figure, $\triangle ABC$ has
 $DE \parallel AC$.

Then, by using Basic Proportionality
Theorem:

$$\frac{AD}{BD} = \frac{CE}{BE}$$

$$\Rightarrow \frac{3}{3} = \frac{4}{x} \Rightarrow 3x = 12$$

$$\Rightarrow x = \frac{12}{3} = \boxed{4} \text{ Ans}$$

Therefore, we obtain, $x = 4$

Qus. 15 Ans...

(a) ⇒ To find probability of drawing
an ace card from well shuffled
deck of 52 cards; $P(E)$

We know,

total possible outcome = 52; as there
are total 52 cards

Also, there are total 4 set in a
deck, each set has one ace

i.e. ⇒ $P(E) = \frac{\text{total favourable outcome}}{\text{total possible outcome}}$

$$\Rightarrow P(E) = \frac{4}{52} = \left[\frac{1}{13} \right] \text{ Ans}$$

(b) \Rightarrow a red card.

Then Out of 4 deck set in a deck, 2 sets
are of red cards each of 13 cards
count

Total red cards in a deck = 2×13
= 26

Therefore, $P(E) = \frac{26}{52} = \left[\frac{1}{2} \right]$ Ans.

Qus. 16 Ans...

\Rightarrow We need to prove, $\sqrt{7}$ is irrational

Let us assume, $\sqrt{7}$ is rational
[By proof of contradiction;]

Then, $\sqrt{7}$ can be written in the form

$$p/q \Rightarrow \sqrt{7} = \frac{p}{q}$$

[If we p & q have common factor other than 1, then we can divide p & q by that no.]

Thus, we have p & q as co-prime

i. $\Rightarrow \sqrt{7} = \frac{p}{q} \quad (q \neq 0)$

$$q\sqrt{7} = p$$

$$7q^2 = p^2 \rightarrow \textcircled{1}$$

\Rightarrow This shows that p^2 is divisible by 7, and if p^2 is divisible then 'p' will also be divisible by 7 (by theorem)

Now, let, $p = 7a$

Then, eqⁿ 1 become,
 $7q^2 = (7a)^2$

$$\Rightarrow 7q^2 = 49a^2$$

$$\Rightarrow q^2 = 7a^2 \rightarrow \textcircled{2}$$

This shows that q^2 is divisible by 7, and same q also.

From above, eqⁿs we obtain,

'7' as common factor of p & q
But this contradicts to fact that they're co-prime.

This contradiction has arisen due to our false assumption,

Hence, our assumption is false, thus, we can conclude that

$\sqrt{7}$ is irrational.

Qus. 17 Ans...

⇒ Given, quadratic equation: (has equal roots)

$$(a-12)x^2 + 2(a-12)x + 2 = 0$$

To find value of 'a'

Since, equation has two equal roots ⇒

$$b^2 - 4ac = 0$$

$$\text{Here, } b = 2(a-12) = 2a-24$$

$$a = a-12$$

$$c = 2$$

Thus, we can write,

$$(2a-24)^2 - 4(a-12)(2) = 0$$

$$\text{i.e. } (4a^2 + 576 - 96a) - 8a + 96 = 0$$

$$\Rightarrow 4a^2 + 672 - 104a \text{ or } 4a^2 - 104a + 672$$

Dividing eqⁿ by '4'

$$\Rightarrow a^2 - 26a + 168 = 0$$

$$\Rightarrow a^2 - 12a - 14a + 168 = 0$$

$$\Rightarrow a(a-12) - 14(a-12) = 0$$

$$\Rightarrow (a-12)(a-14) = 0$$

$$\begin{array}{l} \text{for, } a-12=0 \quad ; \quad [a=12] \\ \text{for, } a-14=0 \quad ; \quad [a=14] \end{array} \quad \underline{\underline{AM}}$$

The req. value of 'a' can be either 12
or 14

[Qus. 18 Ans...]

⇒ Given, equations :

$$\frac{1}{x} + \frac{2}{y} = 3 \rightarrow \textcircled{1} \text{ eq}^n$$

$$\frac{2}{x} - \frac{4}{y} = 2 \rightarrow \textcircled{2} \text{ eq}^n$$

Let, $\frac{1}{x} = A$ & $\frac{1}{y} = B$

Then, eqⁿ 1 becomes, ⇒ $A + 2B = 3 \rightarrow \textcircled{3} \text{ eq}^n$
& eqⁿ 2 " ⇒ $2A - 4B = 2 \rightarrow \textcircled{4} \text{ eq}^n$

Multiplying 2 with eqⁿ ③

⇒ $2A + 4B = 6 \rightarrow \textcircled{5} \text{ eq}^n$

On solving eqⁿ 4 & 5 (elimination method)
we obtain $\left[B = \frac{1}{2} \right]$

on putting this value in eqⁿ 3,

we get, $A + 1 = 3$
⇒ $A = 2$

Hence, we have $A = 2$ & $B = \frac{1}{2}$

Now, we have ; $A = \frac{1}{x} = 2 \Rightarrow x = \left[\frac{1}{2} \right] \underline{\underline{Ans}}$

Similarly ; $B = \frac{1}{y} = \frac{1}{2} \Rightarrow y = [2] \underline{\underline{Ans}}$

Qus. 19 Ans..

⇒ Given, first term of an A.P. = 5
Last term same A.P. = 45

$$\Rightarrow a = 5, (a_n) l = 45$$

Also, given, Sum of terms, $S_n = 400$

$$\Rightarrow S_n = \frac{n}{2} [a + l]$$

$$\Rightarrow 400 = \frac{n}{2} [5 + 45]$$

$$\Rightarrow \frac{50n}{2} = 400 \Rightarrow n = \frac{400 \times 2}{50}$$

$$n = \frac{800}{50} = [16] \text{ Ans}$$

To find common difference,

$$a_{16} = a + (16-1)d$$

$$\Rightarrow 45 = 5 + 15d$$

$$\Rightarrow \frac{40}{15} = d \Rightarrow d = \left[\frac{8}{3} \right] \text{ Ans}$$

Therefore, we obtain, total number of terms in A.P. = 16

and common difference of A.P. = $\left[\frac{8}{3} \right]$

[Qus. 20 Ans..]

$$\Rightarrow \text{To prove: } \frac{1 + \sec A}{\sec A} = \frac{\sin^2 A}{1 - \cos A}$$

Taking L.H.S

$$\Rightarrow \frac{1 + \sec A}{\sec A} = \frac{1}{\sec A} + \frac{\sec A}{\sec A}$$

$$\Rightarrow \cos A + 1 \text{ or } [1 + \cos A] \text{ LHS}$$

Taking R.H.S

$$\Rightarrow \frac{\sin^2 A}{1 - \cos A} \quad [\because \sin^2 A = 1 - \cos^2 A]$$

$$\Rightarrow \frac{1 - \cos^2 A}{1 - \cos A} \quad [\because (1)^2 - \cos^2 A = (1 + \cos A)(1 - \cos A)]$$

$$\Rightarrow \frac{(1 + \cos A)(1 - \cos A)}{1 - \cos A} = [1 + \cos A] \text{ R.H.S}$$

We get, $1 + \cos A = 1 + \cos A$

$$\Rightarrow \text{L.H.S} = \text{R.H.S}$$

Hence proved!

Ques. 21 Ans...

\Rightarrow Given coordinates A(-1, 7) & B(4, -3) forming a line segment,

Let a line segment = AB

* Let (x, y) be the coordinate which

divides AB in the ratio 2:3

Thus, $m_1 : m_2 \Rightarrow 2 : 3$

Then, by using section formula, ^{for} (x, y)

$$x = \left[\frac{m_1(x_2) + m_2(x_1)}{m_1 + m_2} \right]$$

$$y = \left[\frac{m_1(y_2) + m_2(y_1)}{m_1 + m_2} \right]$$

$$\Rightarrow x = \left[\frac{2(4) + 3(-1)}{2+3} \right] \Rightarrow \frac{8-3}{5} = \frac{5}{5} = \boxed{1}$$

$$\Rightarrow y = \left[\frac{2(-3) + 3(7)}{2+3} \right] \Rightarrow \frac{-6+21}{5} = \frac{15}{5} = \boxed{3}$$

∴, required coordinate $(x, y) = (1, 3)$
Solution

[Qus. 22 Ans...]

⇒ Given, a point on x -axis which is equidistant from $(2, -5)$ & $(-2, 9)$

Let, that point be $P(x, y)$ ⇒ since it lies on x -axis ⇒ $(x, 0)$ i.e. $P = (x, 0)$

Let, $A = (2, -5)$ & $B = (-2, 9)$

According to question,

$$AP = BP \rightarrow \textcircled{1}$$

Using distance formula;

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\text{eq(1)} \Rightarrow \sqrt{(2-x)^2 + (-5-0)^2} = \sqrt{(-2-x)^2 + (9-0)^2}$$

On squaring both sides

$$\Rightarrow (2-x)^2 + (-5)^2 = (-2-x)^2 + (9)^2$$

$$\Rightarrow 4 + x^2 - 4x + 25 = 4 + x^2 + 4x + 81$$

$$\Rightarrow -4x - 4x = 81 - 25$$

$$-8x = 56$$

$$x = \frac{56}{-8} = [-7]$$

Therefore required coordinate $(x, 0) = [(-7, 0)]$

[Qus. 23 Ans...]

\Rightarrow In the provided figure;

side of square ABCD = 14 cm

Then, its area = Side \times side

$$= 14 \times 14$$

$$\text{Area of square} = [196 \text{ cm}^2]$$

$$\text{Area of semicircle} = \frac{1}{2} \times \pi \times (r)^2$$

In the given semicircle, radius = half of side of square = $\frac{14}{2} = 7 \text{ cm}$

$$\text{Therefore area of semi-circle} = \frac{1}{2} \times \frac{22}{7} \times 7 \times 7$$

$$\Rightarrow \underline{77 \text{ cm}^2}$$

$$\begin{aligned} \text{Then, area of 2 semi circle} &= 2 \times 77 \text{ cm}^2 \\ &= [154 \text{ cm}^2] \end{aligned}$$

It is clear from fig. that :

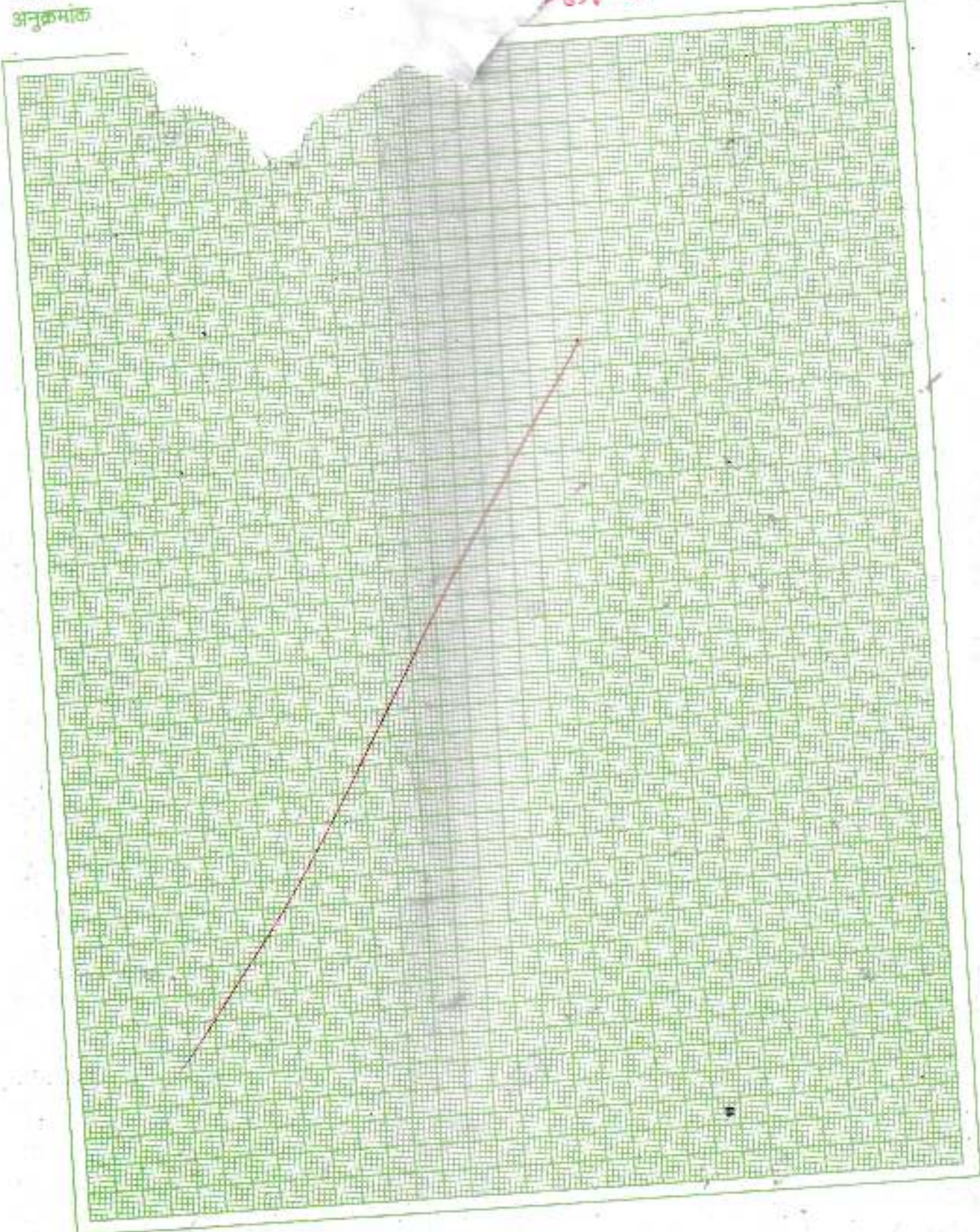
$$\begin{aligned} \text{Area of shaded region} &= (\text{Area of square}) \\ &\quad - (\text{area of } 2 \times \text{semi circles}) \end{aligned}$$

$$\Rightarrow \text{Area of shaded region} = 196 - 154 \Rightarrow \underline{42 \text{ cm}^2} \text{ Solution}$$

$$\text{Hence, area of shaded region} = \underline{\underline{42 \text{ cm}^2}}$$

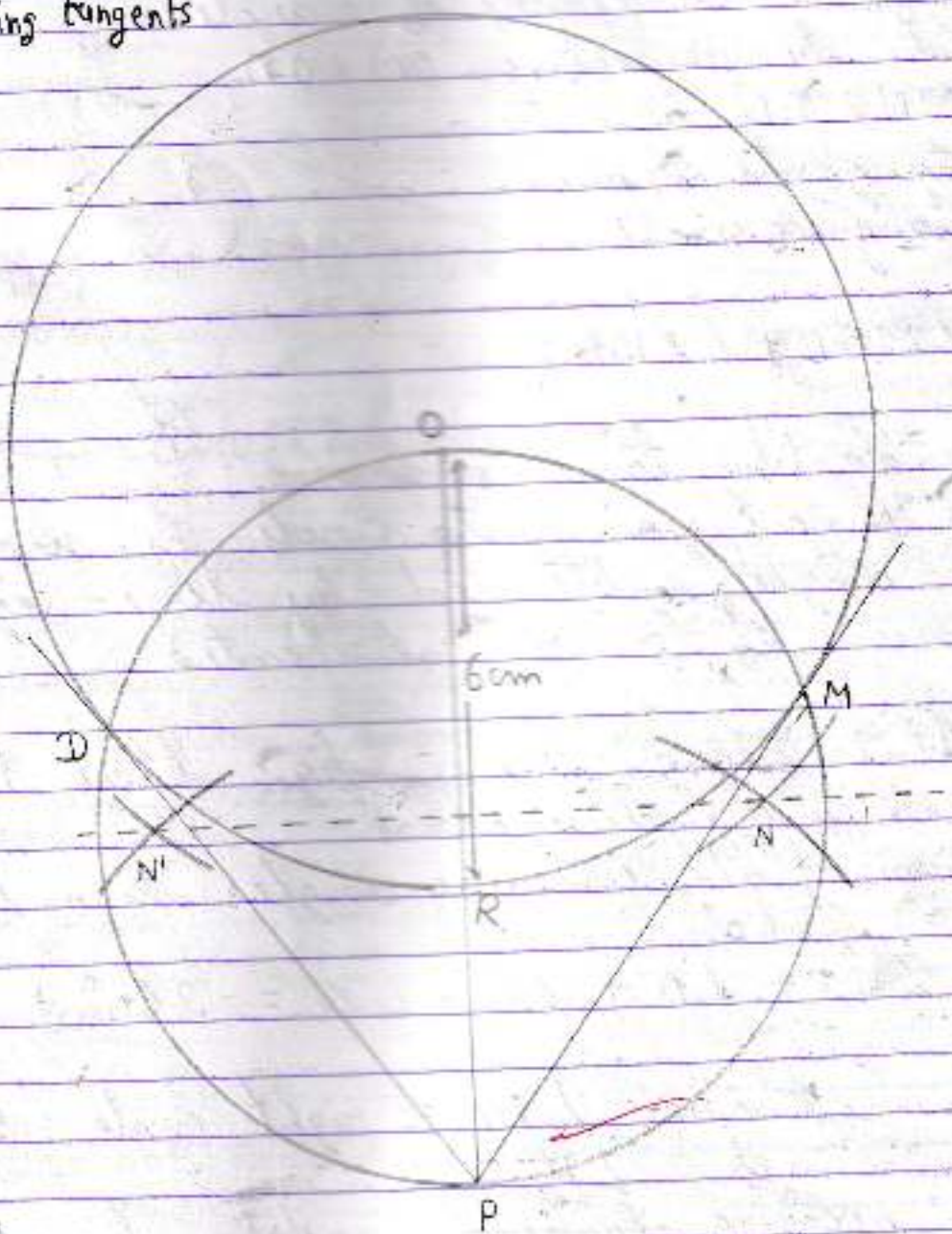
Roll No
अनुक्रमांक

55/24/2022



Qus. 24 Ans...

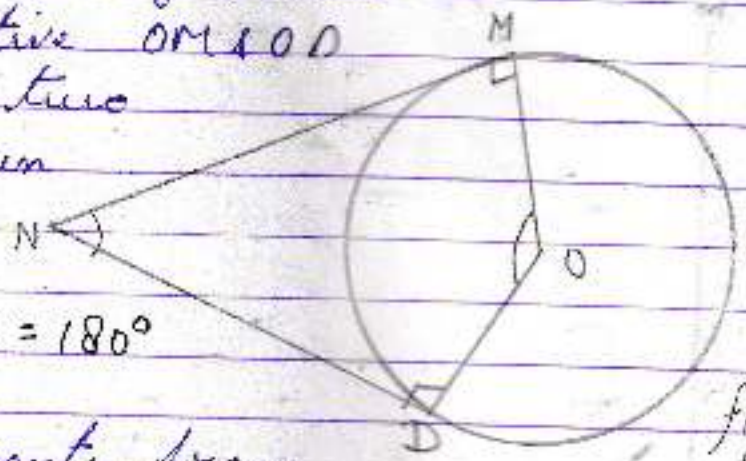
⇒ Drawing tangents



In provided fig., by construction
we have, radius $OR = 6\text{ cm}$
line seg. $OP = 10\text{ cm}$
Therefore, we receive,
tangents PD & PM
such that ; $PD = 8\text{ cm}$
 $PM = 8\text{ cm}$

Qus. 25 Ans...

⇒ Let, O be centre of a circle
its be respective OM & OD
& MN & DN are two
tangents drawn
to given circle.



To prove: $\angle MND + \angle MOD = 180^\circ$

i.e. angle b/w tangents from
external point to circle is supplementary
to angle subtended by line-seg. joining
point of contact at centre.

Proof: It is clear from fig. that $MODN$
is a quadrilateral.

Sum of all interior angles in a quadrilateral
= 360°

$$\angle M + \angle O + \angle N + \angle D = 360^\circ \rightarrow \text{①}$$

Also, we know, $\angle M = \text{right angle} = 90^\circ$
& $\angle D = \text{right angle} = 90^\circ$

[\because because tangents radius drawn to
point of contact form are perpendicular
to tangents i.e. forms 90°]

Putting these values in eqⁿ ①,
we obtain:

$$\Rightarrow 90^\circ + \angle O + \angle N + 90^\circ = 360^\circ$$

$$\Rightarrow \angle O + \angle N = 360^\circ - 90 - 90$$

$$\Rightarrow \angle O + \angle N = 180^\circ$$

Hence, proved that $\angle MND$ and $\angle MOD$ are supplementary!

Qus. 26 Xiv...

\Rightarrow Let the speed of stream be ' x km/hr'
Given, \Rightarrow speed of boat 18 km/hr
& distance = 24 km
Case I: When ^{boat} speed goes upstream
then its speed $\Rightarrow (18-x)$ km/h

Also, Time = $\frac{\text{Distance}}{\text{Speed}}$ [Let time taken be T_1]

$$T_1 = \frac{24}{18-x}$$

Case II: When boat goes downstream
its speed $\Rightarrow (18+x)$ km/h

Let, time taken be T_2

$$\Rightarrow T_2 = \frac{24}{18+x}$$

According to question,
more boat taken 1 hour more
when it goes upstream than
downstream.

This implies that ?

$$\Rightarrow \frac{24}{(18-u)} - \frac{24}{(18+u)} = 1 \quad \text{ie } T_1 - T_2 = 1$$

$$\Rightarrow \frac{24(18+u) - 24(18-u)}{(18-u)(18+u)} = 1 \quad [\because (a-b)(a+b) = a^2 - b^2]$$

$$\Rightarrow \frac{432 + 24u - 432 + 24u}{(18)^2 - (u)^2} = 1$$

To,

$$\Rightarrow 48u = 324 - u^2$$
$$u^2 + 48u - 324 = 0 \quad [ax^2 + bx + c] \text{ standard form}$$

Using quadratic formula

$$\therefore \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-48 \pm \sqrt{(48)^2 - 4(1)(-324)}}{2(1)}$$

$$\Rightarrow \frac{-48 \pm \sqrt{3600}}{2}$$

$$\Rightarrow \frac{-48 \pm 60}{2}$$

for (+ve) $\frac{-48+60}{2} = \frac{12}{2} = \boxed{6} \text{ km/hr}$

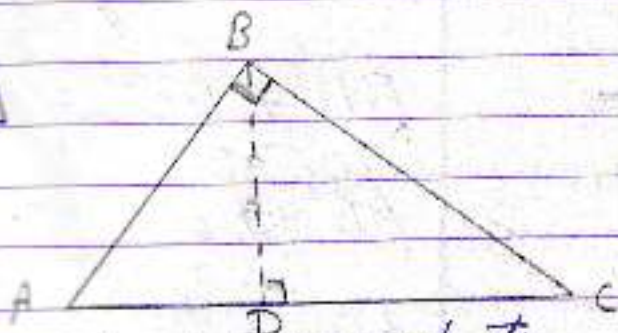
for (-ve) $\frac{-48-60}{2} = \frac{-108}{2} = \boxed{-54}$

Since, speed is a measure, which can't be negative.

Therefore, speed of stream, $u = \boxed{6 \text{ km/hr}}$

Qus 28. Ans...

⇒ Let, ABC be a right Δ
right angled at B



To prove: $AC^2 = AB^2 + BC^2$
i.e. square of hypotenuse is equal to
sum of squares of other 2 sides.

Construction: Draw $BD \perp AC$

Proof: We know, Theorem, that
[∵ If a perpendicular is drawn from vertex
of right angle in a right triangle to
hypotenuse, then triangles formed
on each side are similar to whole
and to each other]

⇒ $\Delta ABD \sim \Delta ACB$

Then, according to Thales theorem

$$\frac{AD}{AB} = \frac{AB}{AC}$$

$$\Rightarrow AC \cdot AD = AB^2 \rightarrow \textcircled{1}$$

Also, $\Delta BDC \sim \Delta ABC$ [from above used theorem]

Then, by Thales theorem:

$$\frac{CD}{BC} = \frac{BC}{AC}$$

$$\Rightarrow CD \cdot AC = BC^2 \rightarrow \textcircled{2}$$

On adding eqⁿ (1) & (2), we obtain

$$AB^2 + BC^2 = AC \cdot AD + AC \cdot CD$$

$$\Rightarrow AB^2 + BC^2 = AC(AD + CD)$$

from fig., we have $AD + CD = AC$

Therefore, $AB^2 + BC^2 = AC(AC)$

$$AB^2 + BC^2 = AC^2$$

Hence, proved! i.e. $AC^2 = AB^2 + BC^2$

i.e. In a right Δ , sq. of hypotenuse
= Sum of sq.s of other 2 sides

Qus. 29 Ans....

\Rightarrow Given, a pipe of diameter = 20 cm

Then, area of its cross-section
= $\pi r^2 = \pi \left(\frac{0.2}{2}\right)^2$

Also, given, a rate of flow of water = 3 km/hr

or $\Rightarrow \frac{3000 \text{ m}}{60 \text{ min}} = 50 \text{ m/min}$

Thus, we can conclude that total water
discharge from pipe in a min

\Rightarrow area of cross section \times speed

$$\Rightarrow \pi (0.1)^2 \times 50 \Rightarrow \pi \times 0.01 \times 50$$

$$\Rightarrow \underline{0.5 \pi \text{ cm}^2}$$

To find time in which tank will be filled;

Let, time taken be 'T'

Given, cylindrical tank : diameter = 10 cm

ht. (depth) = 2 cm

Then, total water in it = its volume

$$\Rightarrow \pi r^2 h = \pi \left(\frac{10}{2}\right)^2 \times 2 = \pi (5)^2 \times 2$$

Arithmetically, time^(T) in which tank will be filled with water by pipe

$$\Rightarrow \pi \times T \times$$

$$\Rightarrow T \cdot 0.5 \pi = \pi (5)^2 \times 2$$

$$= \frac{\pi (5)^2 \times 2}{0.5 \pi} = \frac{5^2 \times 2}{0.5} = \frac{50}{0.5} = \boxed{100} \text{ Min}$$

Thus, in 100 minutes tank will be filled by water. (using pipe) !!

Qus. 30 Ans...

⇒ C. I. (Marks)	0-10	10-20	20-30	30-40	40-50	50-60
No. of students	6	14	10	15	5	10

To find mode:

It is clear from given data that, highest frequency i.e. 15 belong to class interval 30-40.

Hence, C.I.: 30-40 ⇒ ~~class~~ Modal Class

Lower,

Lower limit of modal class, $l = 30$

Frequency of modal class, $f_1 = 15$

Frequency of class preceding modal class, $f_0 = 10$

Frequency of class succeeding modal class, $f_2 = 5$

Difference b/w upper & lower limit of modal class, i.e. $40 - 30$, $h = 10$

Now, we know:

$$\text{Mode} = l + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h$$

Substituting ^{required} values in provided formula we obtain;

$$\Rightarrow 30 + \left[\frac{15 - 10}{2(15) - 10 - 5} \right] \times 10$$

$$\Rightarrow 30 + \left[\frac{5}{30 - 10 - 5} \right] \times 10$$

$$\Rightarrow 30 + \frac{5}{15} \times 10$$

$$\Rightarrow 30 + \frac{1 \times 10}{3}$$

$$\Rightarrow 30 + \frac{10}{3}$$

$$\Rightarrow 30 + 3.33$$

$$\Rightarrow \boxed{33.33} \text{ Ans}$$

Hence, modes of marks obtained = $\boxed{33.33}$

Que. 27 Ans...

\Rightarrow Given two poles of equal ht.

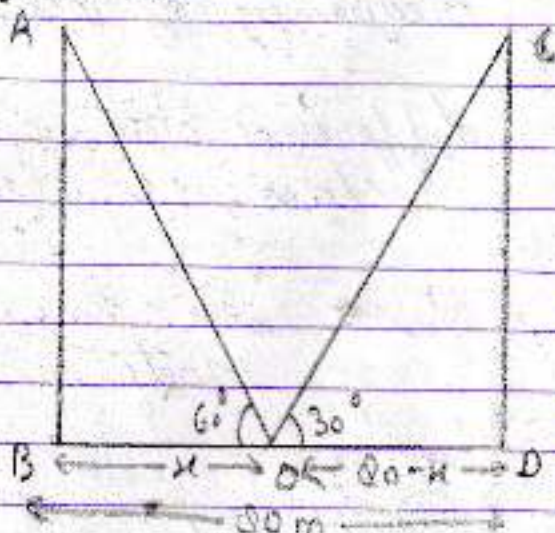
let $AB = CD$

Distance b/w two poles = 80m

& O is point on BD

Let, $BO = x$ metre

$DO = 80 - x$ metre.



Also given, respective angle of elevation b/w them.

Now, from fig.

$$\text{In } \triangle ABO, \tan 60^\circ = \frac{AB}{BO}$$

$$\Rightarrow \sqrt{3} = \frac{AB}{x} \Rightarrow x = \frac{AB}{\sqrt{3}} \text{ or } BO = \frac{AB}{\sqrt{3}} \quad \text{--- (1)}$$

$$\text{In } \triangle COD, \tan 30^\circ = \frac{CD}{DO}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{CD}{80-x} \Rightarrow 80-x = CD\sqrt{3} \text{ or } DO = CD\sqrt{3} \quad \text{--- (2)}$$

$$\text{We know, } BO + DO = 80$$

\Rightarrow from eq (1) & (2) we substitute value of BO & DO

$$\Rightarrow \frac{AB}{\sqrt{3}} + CD\sqrt{3} = 80$$

$$\Rightarrow \frac{AB + CD\sqrt{3}(\sqrt{3})}{\sqrt{3}} = 80$$

$$\Rightarrow AB + 3CD = 80\sqrt{3}$$

$$\Rightarrow 4AB = 80\sqrt{3}$$

$$AB = \frac{80\sqrt{3}}{4} = 20\sqrt{3} \quad [\because AB = CD \text{ given}]$$

Hence ht. of ~~two~~ ^{each} poles = $20\sqrt{3}$ m

$$\text{Now, we know, } x = \frac{AB}{\sqrt{3}} = \frac{20\sqrt{3}}{\sqrt{3}} = 20$$

We get, $x = 20$ m = BO

Also, $DO = 80 - x$

$DO = 80 - 20 = \underline{60 \text{ m}}$

Hence, height of each pole = $20\sqrt{3} \text{ m}$

distance of $BO = 20 \text{ m}$

" " $DO = 60 \text{ m}$

Answer